The following BASIC code generates 10,000 values of a random variable $X$ and calculates the sample average, the sample variance, and the fraction of sample values that lie in the interval ( $a, b]$. Adapt this simulation program to:

1. Calculate the values needed to fill in the table for $E(X), V(X)$ and $P(a<X \leq b)$, where $a=0.9$ and $b=1.8$. Show all theoretical calculations.
2. For each case, on a separate page, draw the graph of the theoretical distribution function $F_{x}(t)$, fill in the table describing $F_{x}(t)$, and plot the simulation values given in the table on the same graph as the theoretical distribution function.
```
RANDOMIZE
100 INPUT a,b
200 FOR i = 1 TO 10000
generate X
300 S1 = S1 + X
400 S2 = S2 + X^2
500 IF (X > a) AND (X <= b) THEN c = c + 1
600 NEXT i
700 PRINT S1/10000, S2/10000 -(S1/10000)^2, c/10000
```

| $E(X)$ |  |  |  |  |  |  |  |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Case | $X$ | theory | simulation | theory | simulation | theory | simulation |
| 1 | $X \sim U(0,1)$ |  |  |  |  |  |  |
| 2 | $X \sim \exp (2)$ |  |  |  |  |  |  |
| 3 | $P(X=1 / 2)=1$ |  |  |  |  |  |  |
| 4 | $P(X=0.3)=0.8$ <br> $P(X=1.3)=0.2$ |  |  |  |  |  |  |

Distribution Function $F_{x}(t)$

|  | 1 |  | 2 |  | 3 |  | 4 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $t$ | theory | simulation | theory | simulation | theory | simulation | theory | simulation |  |
| -0.25 |  |  |  |  |  |  |  |  |  |
| 0.00 |  |  |  |  |  |  |  |  |  |
| 0.25 |  |  |  |  |  |  |  |  |  |
| 0.50 |  |  |  |  |  |  |  |  |  |
| 0.75 |  |  |  |  |  |  |  |  |  |
| 1.00 |  |  |  |  |  |  |  |  |  |
| 1.25 |  |  |  |  |  |  |  |  |  |
| 1.50 |  |  |  |  |  |  |  |  |  |

